



INVESTMENT REVERSIBILITY AND COORDINATION FAILURES

Esteban Hnyilicza
CIE-USMP

Encuentro de Economistas BCRP
Abril 2006

HISTORY OF ECONOMIC THOUGHT ACCORDING TO OLIVER WILLIAMSON

-Adam Smith (Lens of Choice)

-Oliver Williamson (Lens of Contract)

AN (IMPROVED) HISTORY OF ECONOMIC THOUGHT

-Adam Smith (Lens of Choice)

-Friedrich von Hayek (Economics as Adaptation to Uncertainty)

-Oliver Williamson (Lens of Contract)

MODEL AND RESULTS

Objectives and Summary

- Bilateral contract with exogenous uncertainty
- Technologies parametrized by reversibility
- Surplus allocated by ex-post bargaining
- Bargaining power related to outside options
- Computation of threshold frontier separating regimes by equilibrium behavior
- Two regimes: cooperation failure and coordination failure

Bayes-Nash Two-Stage Game

- $\theta < \theta^*$ Cooperation failure
Single Pareto-inefficient equilibrium
Prisoner's Dilemma
- $\theta > \theta^*$ Coordination failure
Two equilibrium points
Pareto-inefficient equilibrium dominates

- TRADITIONAL TRADE-OFFS:
(Technology space)

Higher reversibility:

Lower productivity but higher flexibility and capacity for adaptation

- NEW TRADE-OFF:
(Institutional design space)

Higher reversibility:

Options for design of mechanisms to coordinate on efficient equilibrium.

DEVELOPMENT & CONTRACT THEORY

- Clusters, global value chains

- Public-private partnerships

- Organizations and Institutions as Networks of
Implicit Contracts

Complete contracts (Agency theory)

- Incentive vs Insurance

- Efficiency vs information rents

- Renegotiation-proofness

Incomplete contracts

- Ex-ante vs ex-post efficiency

- Hold-up

- Renegotiation protocols as completion rules

Incomplete Contract Theory

HOLD-UP PROBLEM

Ex-post opportunism

Under-investment bias (ex-ante inefficiency)

Williamson (1975), Grossman-Hart-Moore (1985)

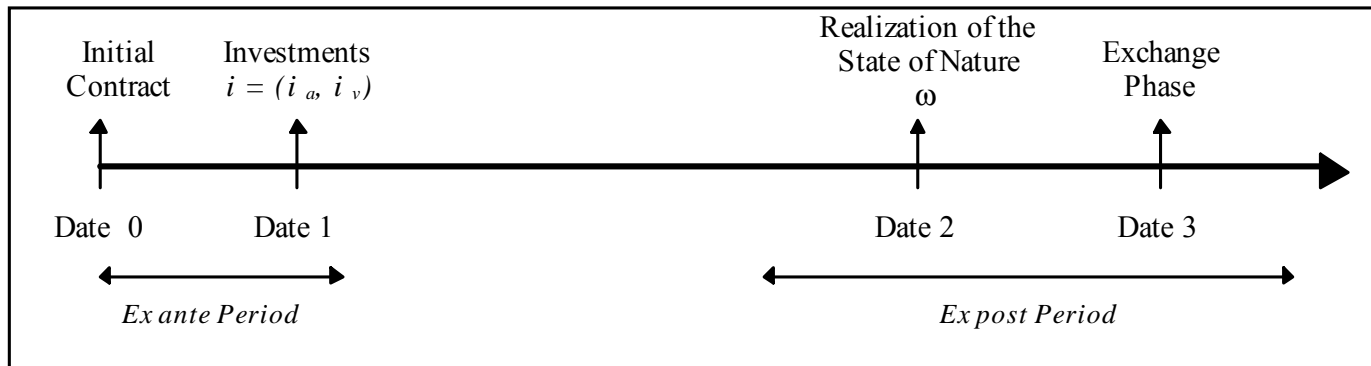
SELF-ENFORCEMENT

Relational contracts

Reputation and trust

Legal structures and endogenous enforcement

Klein (1978), Baker-Gibbons-Murphy (2000, 2004)





Ex -ante efficiency: optimal level of investment

Ex -post efficiency: trade only when it is gainful

Trade-off between commitment and flexibility:

Commitment :


Ex –ante efficiency but may impair ex -post efficiency—commit to an exchange that is not gainful.

Flexibility:

Ex--post efficiency but may impair ex –ante efficiency (hold-up)

Incomplete Contract Theory

- ❑ Coase (1937)
- ❑ Williamson (1975, 1985) Lens of Contract, TCE
- ❑ Incomplete ICT Hart Moore—based on explanation of hold-ups, property rights approach
- ❑ Vertical Integration as partial solution to hold-up
- ❑ Does not achieve first-best because of non-verifiability
- ❑ Supported by Williamson, NIE
- ❑ Challenged by Tirole—revelation mechanisms

- 
-
- “Unbundling Institutions,” Acemoglu (2002)
 - “Trade and Contract Enforcement” Anderson (2002)
 - “Demand for Contract Enforcement and Gains from Trade,” Rubinchik & Samaniego (2005)



□ Investment Reversibility—Single Agent

□ Asset Specificity---Bilateral Contracting

A.S. = Value of quasi-rents within
relationship

= gap relative to next-best
alternative use

Parametrization of Reversibility θ

θ is reversible fraction, $0 \leq \theta \leq 1$.
Fraction θ can be redeployed . Fraction $(1-\theta)$ is a sunk cost.

Date 0: Invest 1 unit

Date 1: Uncertain state realized

Prob (s_{good}) = p , return r_s

Prob (s_{bad}) = $1-p$, return $R_f < r_s$

Date 2: If s_{bad} obtains, redeploy fraction θ to outside option r^* , $R_f < r^* < r_s$

$$E[V] = p \cdot r_s + (1-p) \cdot R_f (1-\theta) + (1-p) \cdot r^* \cdot \theta$$

NUMERICAL EXAMPLE

Investment in a production facility:

Cost \$80M

Gross Revenues \$ 130M with $p = 1/2$
\$ 50M with $p = 1/2$

Reversibility θ

Reservation payoff $r^* = \$100M$

$$E[NPV_{\theta}] = 25\theta + 10$$

$$E[NPV_w] = 25$$

Invest Now vs. Wait to Invest

No-arbitrage condition:

$$E[\text{NPV}_\theta] = E[\text{NPV}_w]$$

$$25\theta + 10 = 25$$

$$\theta^* = 0.6$$

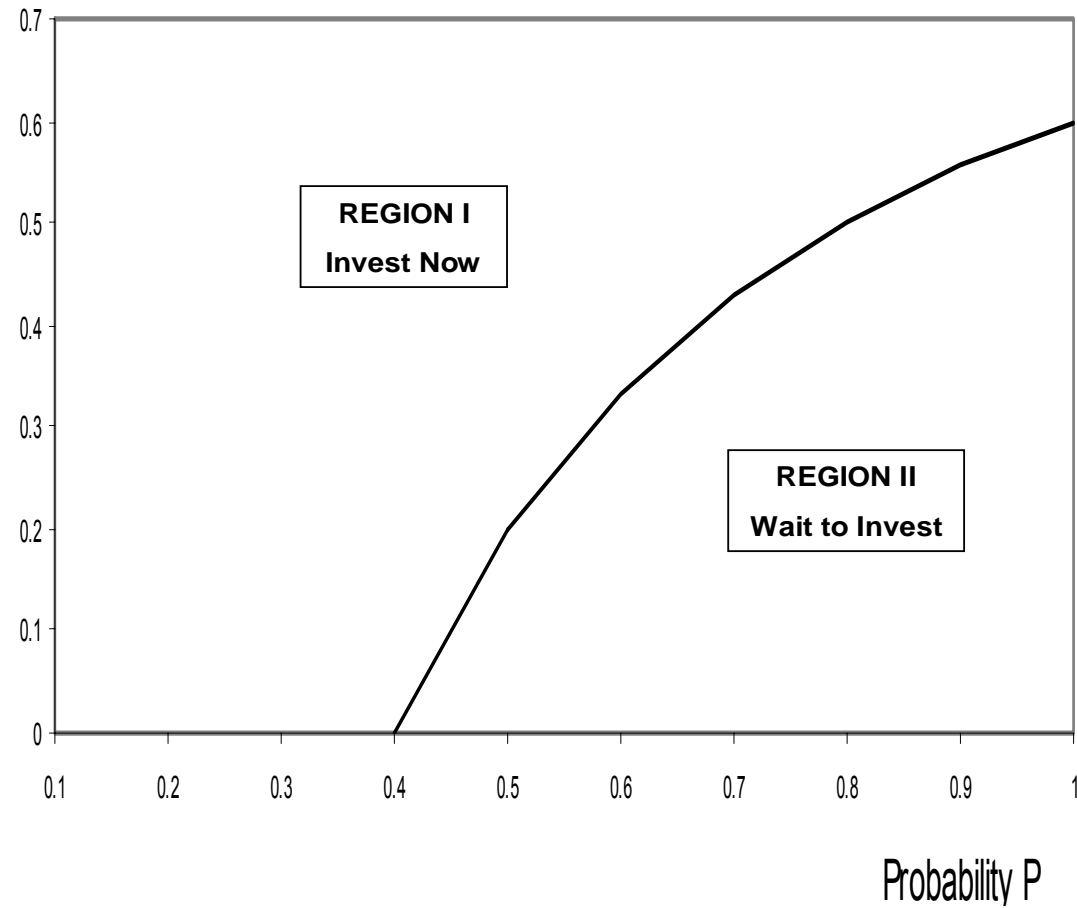
Region I: Invest Now:

$$\theta > 0.6$$

Region II: Wait to Invest

$$\theta < 0.6$$

Reversibility θ



Partial Reversibility and the Decision to Invest

-
- Contract Game with a Continuum of Technologies-- θ_B, θ_S

 - Canonical Contract Game
 - Partially Reversible θ
 - Irreversible ($\theta=0$)

-
- (1) Olcina, G. & Peñarrubia, C., (2002)
"Specific investments and coordination failures"
Deterministic, exogenous technologies
 - (2) Muthoo, A., (1998)
"Sunk Costs and the Inefficiency of Relationship-Specific Investment,"
Deterministic cost structure, focus on bargaining protocol
 - (3) Caballero, R., and Hammour, M.L. (2000)
"Creative Destruction and Development"
Creative destruction
Adjustment costs proportional to degree of irreversibility

Bilateral Contract with a Continuum of Technologies

- The contract game has two stages: the *investment stage* and the *bargaining stage*.
- In the first stage, the buyer and the seller each invest in a technology selected from $T = \{T(\theta), 0 \leq \theta \leq 1\}$. The cost of technology $T(\theta)$ is $c(\theta)$, $c'(\theta) \leq 0$, $c''(\theta) \geq 0$.
- Payoff to investment in technology $T(\theta)$ contingent on random state s . There are two states, $s = s_g$ (*good*) with probability p and $s = s_b$ (*bad*), with probability $1 - p$.

- STAGE II: Bargaining Stage
 - STAGE I: Investment Stage
-

- Investment decisions:

Maximize the expected value of the share of the surplus given expectations about the bargaining outcome in the second stage.

KEY TRADE-OFF

- Higher reversibility θ yields lower productivity, but is associated with higher outside options, implying increased bargaining strength

Stage II: The Bargaining Stage

$$\square \Lambda = E[V(\theta_B, \theta_S)] = p \cdot Rg(\theta_B, \theta_S) + (1-p) [(1-\theta_B)R_f + (1-\theta_S)R_f] \\ + (1-p) [\theta_B r(\theta_B) + \theta_S r(\theta_S)] - c(\theta_B) - c(\theta_S)$$

$$\square J_B(\theta_B, \theta_S) = \omega_B + \frac{1}{2} [\Lambda + \omega_B - \omega_S] \\ = \frac{1}{2} \Lambda - \frac{1}{2} [\omega_B - \omega_S]$$

$$\square J_S(\theta_B, \theta_S) = \omega_S + \frac{1}{2} [\Lambda + \omega_S - \omega_B] \\ = \frac{1}{2} \Lambda - \frac{1}{2} [\omega_S - \omega_B]$$

Given that $\partial\omega_B/\partial\theta_B \geq 0$, $\partial\omega_S/\partial\theta_S \geq 0$, higher reversibility, associated with higher outside options, yields increased bargaining strength

Investment Stage

$$\theta_B^* = \arg \max_{\theta_B} \left\{ \max_{\theta_S} \frac{1}{2} \left[p \cdot R_g(\theta_B, \theta_S) + (1-p) \left[(1-\theta_B)R_f + (1-\theta_S)R_f \right] \right. \right. \\ \left. \left. + (1-p) \left[\theta_B r(\theta_B) + \theta_S r(\theta_S) \right] - c(\theta_B) - \frac{1}{2} \cdot [\omega_B - \omega_S] \right] \right\}$$

$$\theta_S^* = \arg \max_{\theta_S} \left\{ \max_{\theta_B} \frac{1}{2} \left[p \cdot R_g(\theta_B, \theta_S) + (1-p) \left[(1-\theta_B)R_f + (1-\theta_S)R_f \right] \right. \right. \\ \left. \left. + (1-p) \left[\theta_B r(\theta_B) + \theta_S r(\theta_S) \right] - c(\theta_B) - \frac{1}{2} \left[\omega_S - \omega_B \right] \right] \right\}$$

Linear-Quadratic Bayes-Nash Equilibrium

Let

$$R_g(\theta_B, \theta_S) = 1 - (\theta_B + \theta_S) - a(\theta_B - \theta_S)^2$$

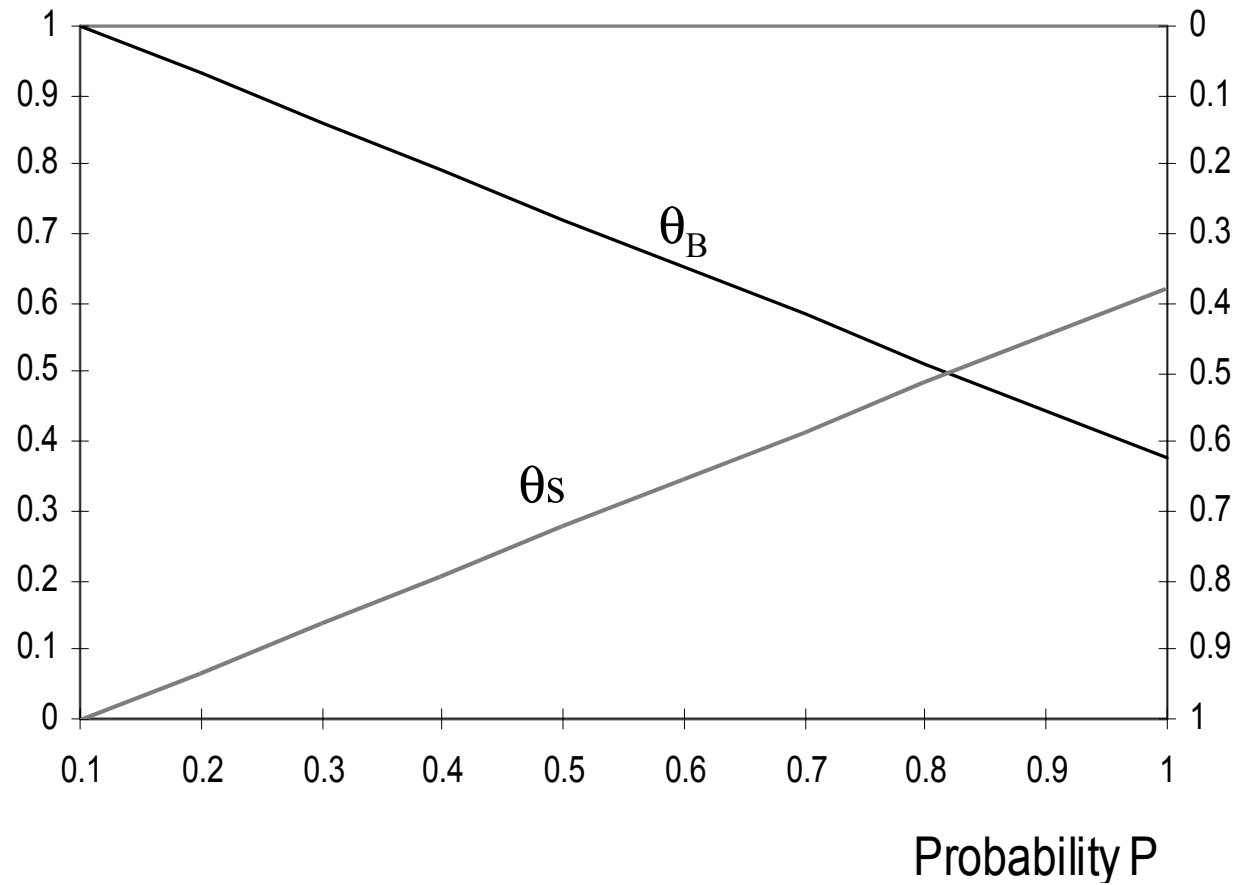
$$\text{and } c(\theta_S) = c(1 - \theta_S)^2, c(\theta_B) = c(1 - \theta_B)^2, r(\theta_B) = r_B, r(\theta_S) = r_S.$$

The optimal investment strategy (θ_B^*, θ_S^*) , is the Nash equilibrium to the game, which solves:

- $\partial J_B(\theta_B, \theta_S) / \partial \theta_B = 2 p a (\theta_S - \theta_B) + (1-p) (r_B - R_f) + 4c (1-\theta_B) - p = 0$
- $\partial J_S(\theta_B, \theta_S) / \partial \theta_S = 2 p a (\theta_B - \theta_S) + (1-p) (r_S - R_f) + 4c (1-\theta_S) - p = 0$

Buyer Reversibility θ_B

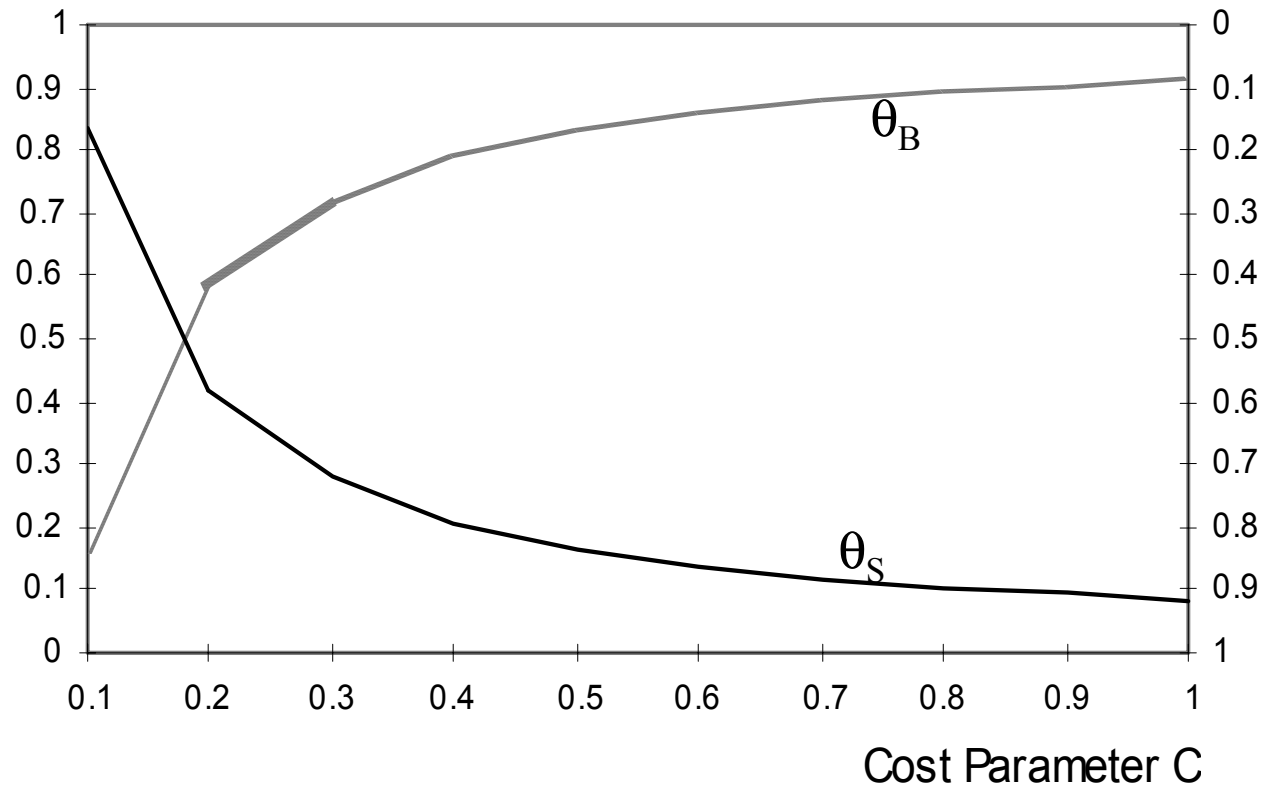
Seller Reversibility θ_S



Bayes – Nash Equilibrium Values

Buyer Reversibility θ_B

Seller Reversibility θ_S



Bayes – Nash Equilibrium Values

The Canonical Contract Game

State-contingent contractual agreement specifying an investment stage and a bargaining stage.

First Stage--Investment

Buyer and seller choose between two technologies:

- H– Hi-tech, specific, irreversible , $\theta = 0$
Outside option 0
- General low-tech (L), partial reversibility
parameter θ , $0 < \theta \leq 1$. Outside option ω

Second Stage--Bargaining

Joint surplus determined by the pair of investments chosen in the first stage.

-
- Cost of high-tech investment = c
 - Cost of low-tech investment = $\psi = c(1-\theta)$

Backward induction:

Bargaining Stage:

Sub-Game I: H,H

Sub-Game II: H,L; L,H

Sub-Game III: L,L

Investment Stage:

Coordination Game/Prisoner's Dilemma

□ *Subgame 1: Both players invest in High-Tech*

Both outside options are zero. The expected payoff is:

$$E[V^{HH}] = p R_g^{HH} + (1-p) R_f ; \quad R_g^{HH} > R_f$$

and the share of the surplus accruing to each party is given by:

$$J^{HH} = \frac{1}{2}[E[V^{HH}]] = \frac{1}{2}[p R_g^{HH} + (1-p) R_f]$$

Subgame 2: One player invests in High-Tech and the other in Low-Tech

$$J_{HL}^B = \frac{1}{2}[E[V^{HL}] - \omega] = \frac{1}{2}[p R_g^{HL} (\theta) + (1-p) R_f (1 - \theta) + (1-p) \cdot \theta r^* - \omega]$$

$$J_{HL}^S = \frac{1}{2}[E[V^{HL}] + \omega] = \frac{1}{2}[p R_g^{LH} (\theta) + (1-p) R_f (1 - \theta) + (1-p) \cdot \theta r^* + \omega]$$

where r^* is the reservation payoff, $R_g^{HH} > r^* > R_f$

$$J_{LH}^B = \frac{1}{2}[E[V^{LH}] + \omega] = \frac{1}{2}[p R_g^{HL} (\theta) + (1-p) R_f (1 - \theta) + (1-p) \cdot \theta r^* + \omega]$$

$$J_{LH}^S = \frac{1}{2}[E[V^{LH}] - \omega] = \frac{1}{2}[p R_g^{LH} (\theta) + (1-p) R_f (1 - \theta) + (1-p) \cdot \theta r^* - \omega]$$

Subgame 3: Both players invest in Low-Tech

Assume symmetric low-tech technologies:

$$\text{i.e. } \theta_B = \theta_S = \theta$$

Then the expected joint payoff is:

$$J_{LL} = E[V_{LL}] = \frac{1}{2}[p R_g^{LL}(\theta) + (1-p) R_f(1 - \theta) + (1-p) \cdot \theta r^* + \omega]$$

SOLUTION CONCEPTS

(1) Subgame perfect equilibrium (Nash):

$$J_{HH} \geq \omega \geq J_{HL}$$

Coordination game: $J_{H,H} \geq J_{L,H}$

Prisoner's Dilemma $J_{HH} \leq J_{LH}$

(2) Focal point—Risk dominance (Harsanyi-Selten)

(3) Repeated games---Trigger Strategies

	H	L
H	J_{HH}, J_{HH}	J_{HL}, J_{LH}
L	J_{LH}, J_{HL}	ω, ω

	H	L
H	$\frac{1}{2} E[V_{HH}] - c, \frac{1}{2} E[V_{HH}] - c$	$\frac{1}{2} E[V_{HL}] - \omega] - c, \frac{1}{2} E[V_{HL}] + \omega] - \psi$
L	$\frac{1}{2} E[V_{LH}] + \omega] - \psi, \frac{1}{2} E[V_{LH}] - \omega] - c$	ω, ω



Threshold Reversibility Frontier

$$\sigma(\theta) = 0, \sigma(\theta) = \Gamma_{HH}(\theta) - \Gamma_{LH}(\theta)$$

$$\sigma(\theta) = 0, \sigma(\theta) = \Gamma_{HH}(\theta) - \Gamma_{LH}(\theta)$$

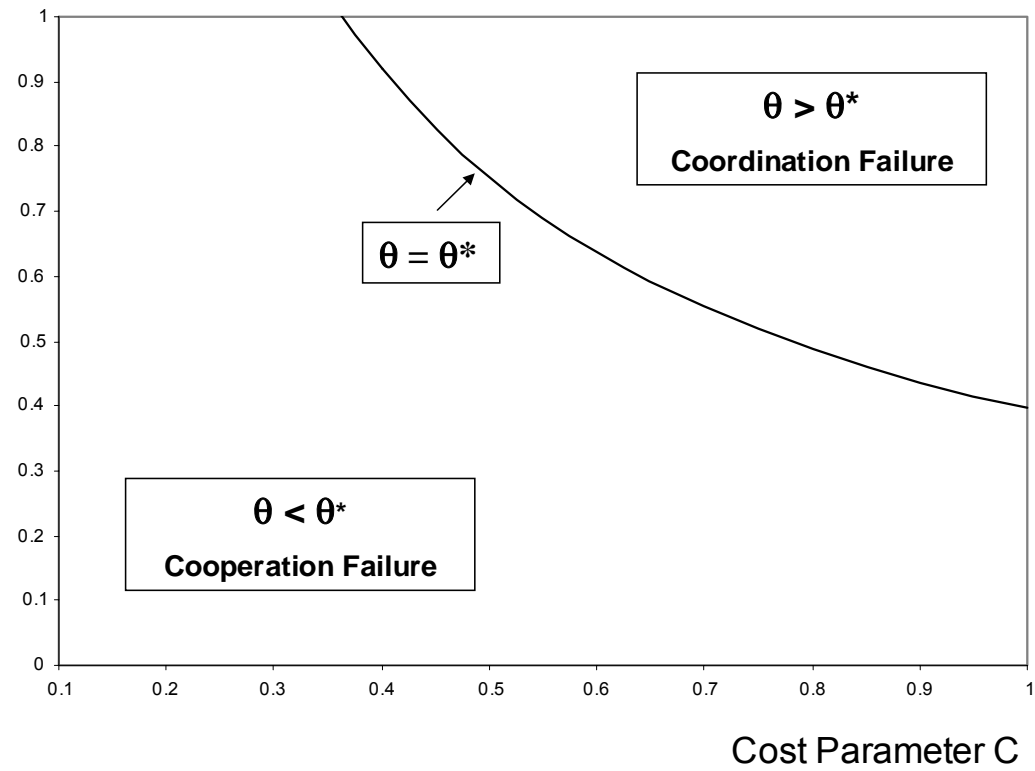
□ *Sub-Regime I*, $R_g^{LH} = (1 - \theta) R_g^{HH}$

$$\theta^* = \{ \omega / [(1-p)(r^* - R_f) - p R_g^{HH} - 2c] \}$$

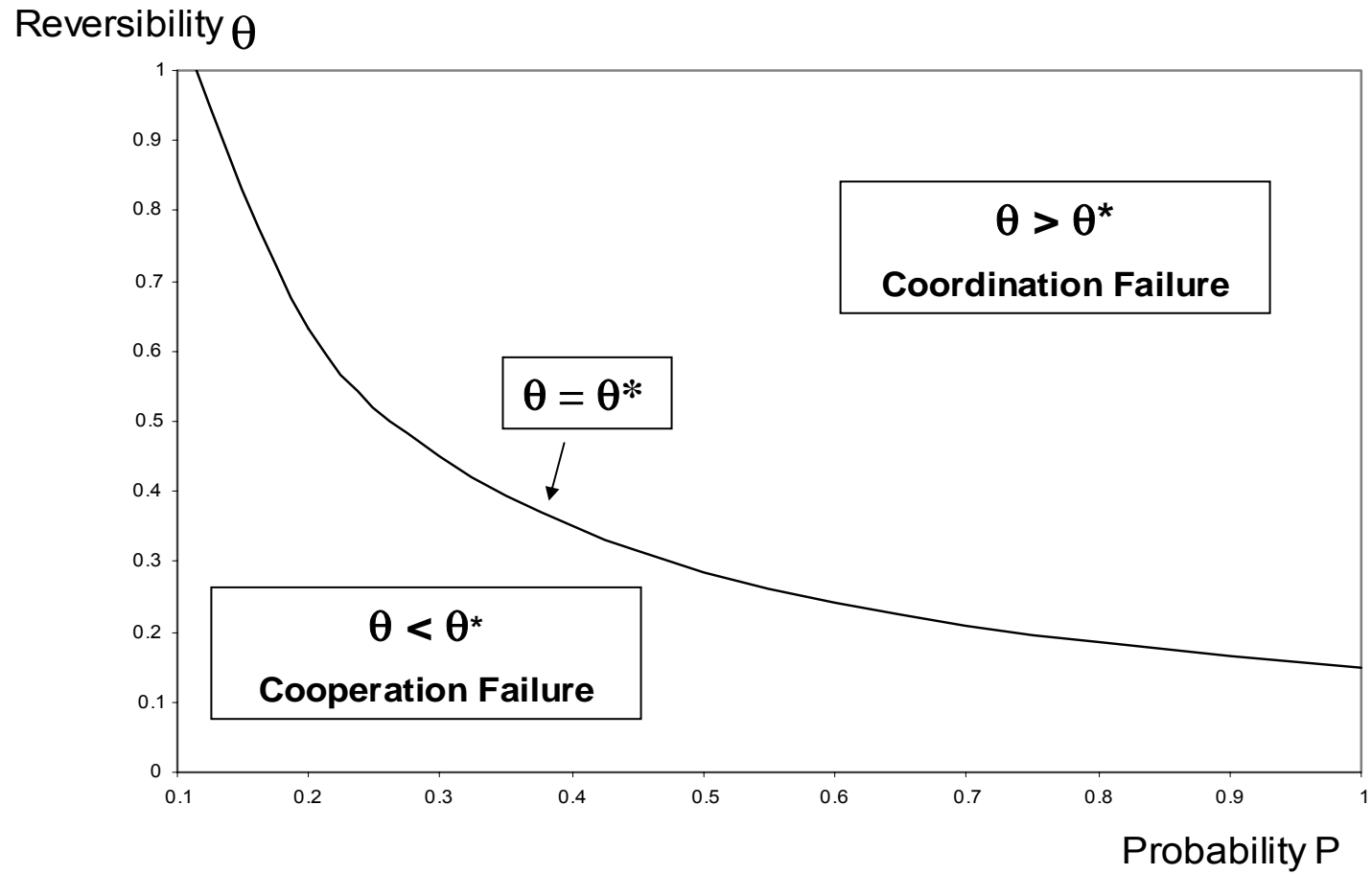
$\theta < \theta^*$ Cooperation failure

$\theta > \theta^*$ Coordination failure

Reversibility θ

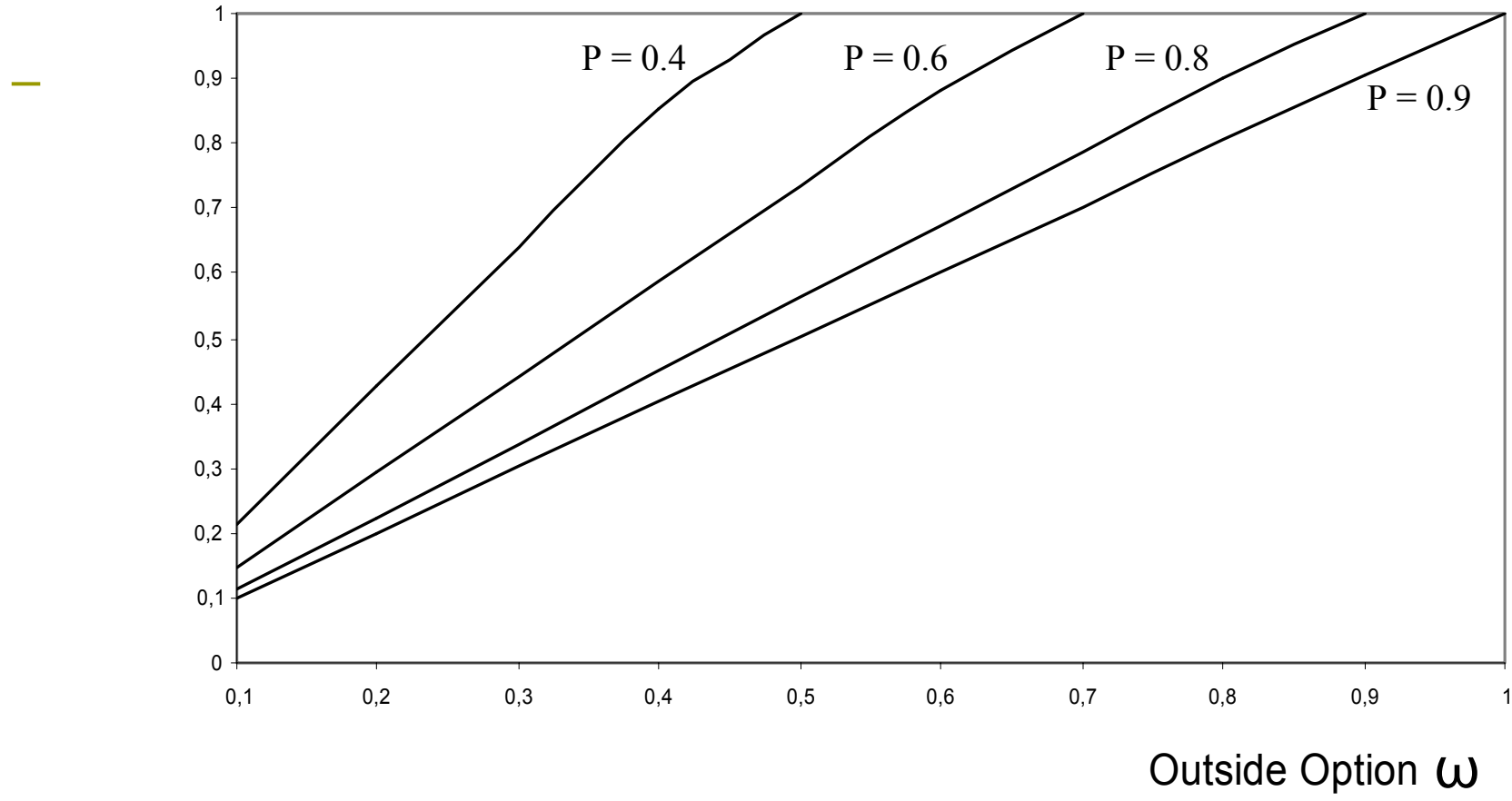


Frontier Values of θ^* at Regime Change



Frontier Values of θ^* at Regime Change

Reversibility θ

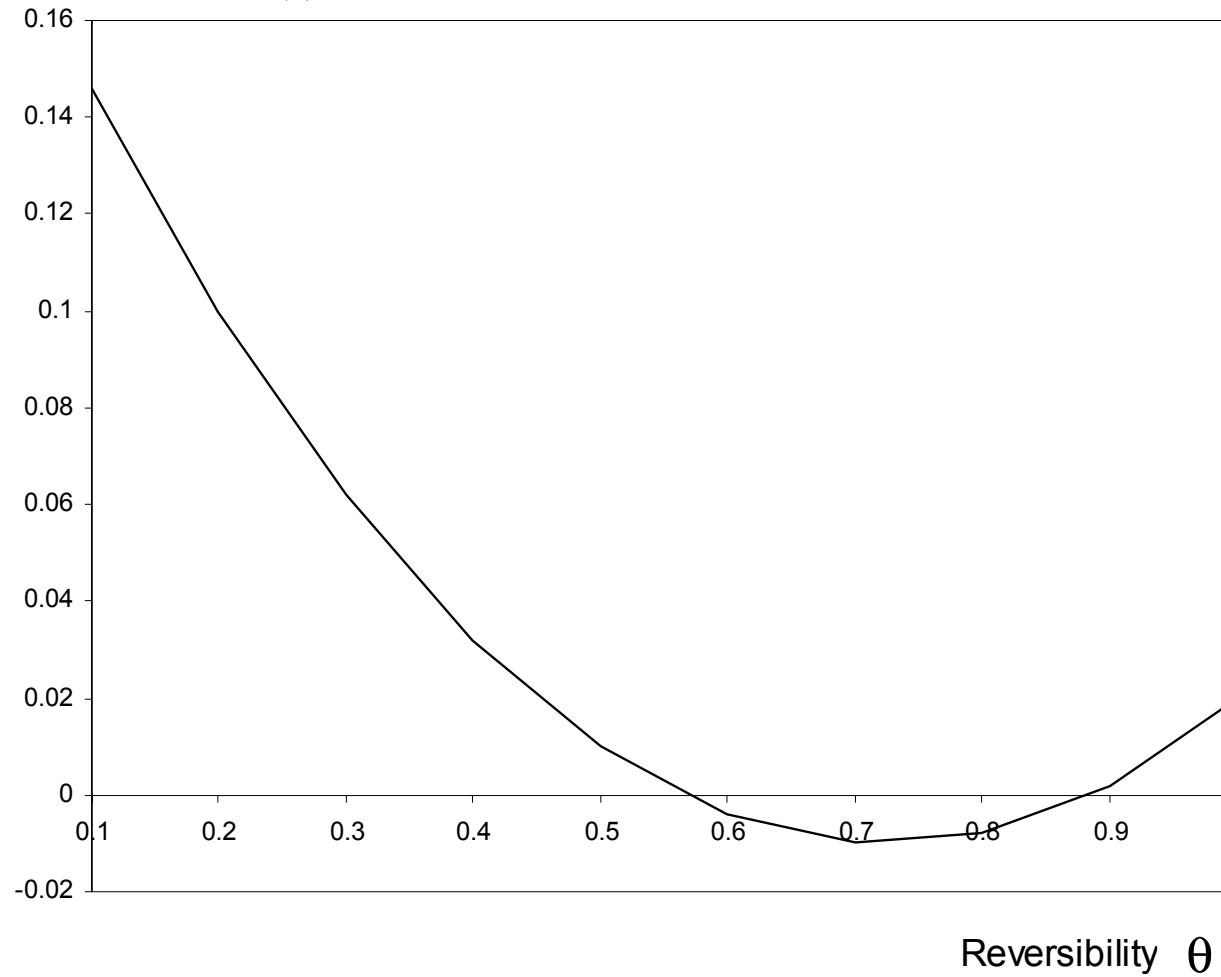


Frontier Values of θ^* at Regime Change

□ *Sub-Regime II, $Rg^{LH} = [a(1, \theta) - \Phi(1, \theta)]$*
 R_g^{HH}

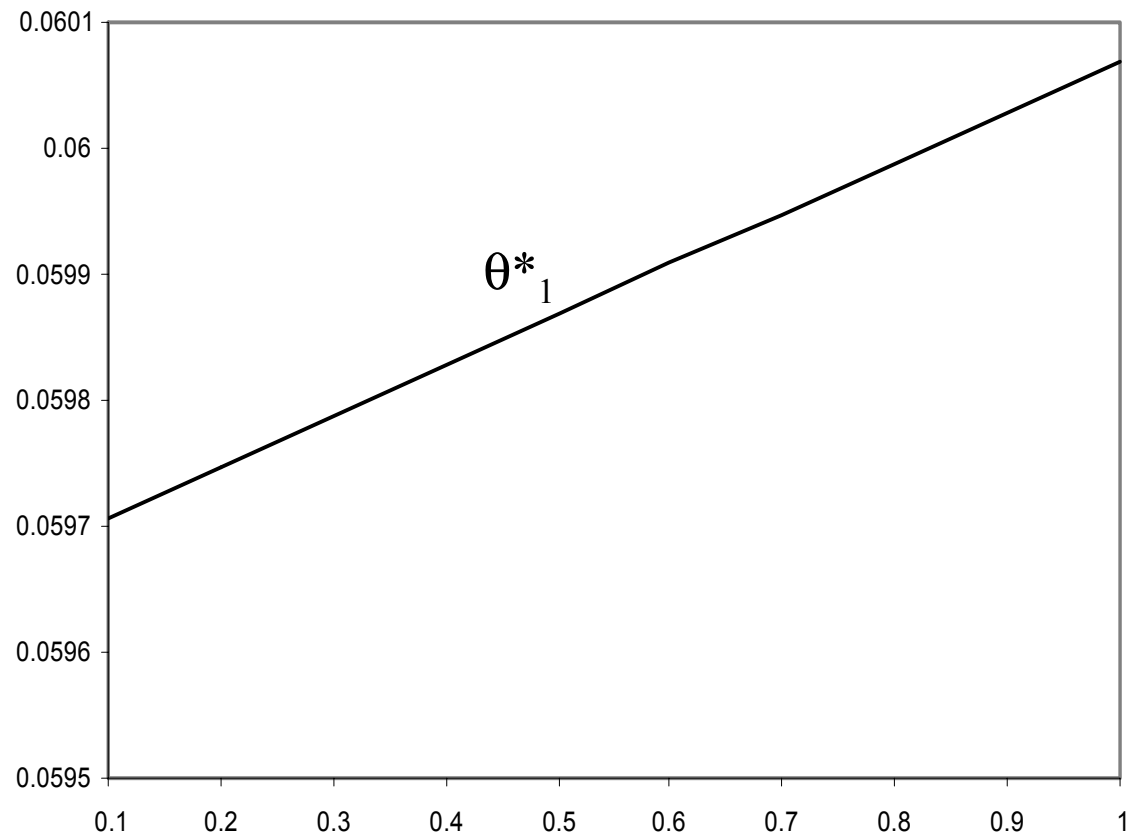
$$\sigma(\theta) = \frac{\gamma Rg^{HH} \theta^2 + [(1-p)(R_f - r^*) + 1 - 2(\gamma + c)] Rg^{HH} \theta + \gamma Rg^{HH} - \omega}{1}$$

Threshold Function $\sigma(\theta)$



Frontier Values of θ^*

Outside Option W



Probability P

CONCLUSIONS

- ❑ Implications of partial reversibility for contract design and performance in the presence of exogenous and strategic uncertainty
- ❑ Explicit modeling of partial reversibility permits examination of trade-offs between commitment and flexibility in organizational design
- ❑ Restructuring and adaptation are facilitated by more flexible and reversible techniques

- 
-
- Reversible and more flexible techniques leave room for policy interventions which enhance efficiency in the presence of weak institutional structures



INVESTMENT REVERSIBILITY AND COORDINATION FAILURES

Esteban Hnyilicza
CIE-USMP

Encuentro de Economistas BCRP
Abril 2006