Estimation and assessment of measures of the natural rate of interest: Evidence from LA economies with inflation targeting *

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* The views expressed here are those of the authors and not necessarily of the BCRP

Erick Lahura (BCRP), José Aguilar (BCRP) y Marco Vega (BC Natural rate of interest: Estimation and assessment



2 Methodology and data



Conclusions

Erick Lahura (BCRP), José Aguilar (BCRP) y Marco Vega (BC Natural rate of interest: Estimation and assessment

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- Era of low interest rates since the global financial crisis, specially in advanced economies, promoted research on the natural rate of interest (NRI).
- Recent period of high inflation has pushed back to higher interest rates.
- Key references: Laubach y Williams (2003) and Woodford (2003).

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- K. Wicksell (1898): The natural rate of interest (NRI) is the rate compatible with a stable price level.
- If $r_t > r_t^n$, lower output and lower prices, and viceversa.
- Woodford (2003) and New Keynesian framework:
 - NRI relates to productivity shocks, consumers' preferences.

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• Taylor rule to achieve NRI and price stability.



- NRI is useful for monetary policiy and financial stability:
 - To determine the stance of monetary policy: if the real shortterm interest rate is below (above) the NRI, then monetary policy is expansive (contractive)
 - To assess potential threatens to financial stability: excessive risk-taking if real interest rates < NRI.

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• Fundamental problem: NRI is unobservable.

Introduction Estimation of the NRI: Several alternatives.

- Univariate filters (HP) or multivariate filters (Kalman filter), combined with theoretical relationships (Laubach y Williams, 2003; Holston et al., 2017, among others).
- Econometric models: TVP-VAR with stochastic volatility (Lubik y Matthes, 2015; Wang y Kwan, 2021, among others) and cointegration (Benati, 2020, 2023).
- Estimation and/or calibration of theoretical models (Doojav and Gantumur, 2020; Zhang et al., 2021). DGSE models (Giammarioli and Valla, 2004; Barsky et al., 2014).
- Borio (2021): indicators of expectations of market participants: e.g. a real forward rate (not control by the CB).



- Estimate and assess two measures of the NRI for Chile and Peru (LATAM, IT).
- Estimation:
 - Time-varying parameter vector autoregression model with stochastic volatility (TVP-VAR-SV), Lubik y Matthes (2015).
 - M1 velocity is the permanent component of the real interest rate Benati (2020, 2023).
- Assessment: Transitory shocks do not affect NRI in the long
 run

	Introduction Methodology and data
	Results
	Conclusions
	Referencias
Contents	





3 Results

Conclusions

Erick Lahura (BCRP), José Aguilar (BCRP) y Marco Vega (BC Natural rate of interest: Estimation and assessment

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- Estimation of NRI: TVP-VAR-SV and Money Velocity
- Asessment: SVAR with long-run restrictions.

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- Proposed by Lubik y Matthes (2015): the rate of growth of GDP, inflation and ex ante real interest rate.
- Bayesian techniques as in Primiceri (2005) and Del Negro y Primiceri (2015).
- The NRI is the conditional long-run (5-year) forecast of the observed ex ante real interest rate.

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• Let $y_t = (g_t, \pi_t, r_t)'$ and 2 lags (TVP-VAR convention). Then:

 $y_t = c_t + B_{1,t}y_{t-1} + B_{2,t}y_{t-2} + u_t$ $t = 1, \dots, T.$

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• The variance covariance matrix Ω_t is descomposed as:

 $\Omega_t = A_t^{-1} \Sigma_t \Sigma_t' A_t^{-1'}$

• $c_t, B_{1,t}, B_{2,t}$ and $Var(u_t) = \Omega_t$ are time varying.

• $u_t \sim N(0, \Omega_t)$



Estimation: TVP-VAR-SV

• Details of
$$\Omega_t = A_t^{-1} \Sigma_t \Sigma_t' A_t^{-1'}$$
:

$$A_t = \begin{pmatrix} 1 & 0 & 0 \\ \alpha_{21,t} & 1 & 0 \\ \alpha_{31,t} & \alpha_{32,t} & 1 \end{pmatrix}, \quad \Sigma_t = \begin{pmatrix} \sigma_{1,t} & 0 & 0 \\ 0 & \sigma_{2,t} & 0 \\ 0 & 0 & \sigma_{2,t} \end{pmatrix}$$

Then, TVP-VAR-SV can be written as:

$$y_t = c_t + B_{1,t}y_{t-1} + B_{2,t}y_{t-2} + A_t^{-1}\Sigma_t\varepsilon_t , \quad t = 1, \dots, T.$$

where $Var(\varepsilon_t) = I_n$.

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- In compact form: $y_t = X'_t B_t + A_t^{-1} \Sigma_t \varepsilon_t$.
- It is assumend that the time varying parameters follow random walk processes:

$$\beta_t = \beta_{t-1} + v_{\beta,t}$$
$$\alpha_t = \alpha_{t-1} + v_{\alpha,t}$$
$$\log \sigma_t = \log \sigma_{t-1} + v_{\sigma,t}$$

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where $u_t, v_{\beta,t}, v_{\alpha,t}, v_{\sigma,t}$ are mutually independent.

Introduction Methodology and data Results Conclusions Referencias Methodology Estimation: TVP-VAR-SV

- Assumptions:
 - Initial states for the coefficients, the covariances, log volatilities and hyperparmeters are independent of each other.
 - Priors for the hyperparameters *Q*, *W* and the blocks of *S* are distributed as independent inverse-Wishart.
 - Normal priors on the entire sequences of B's, α's, and log σ's (conditional on Q, W, and S).

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 Posterior distributions of B, A, and Σ and V are evaluated using Gibbs sampling as in Del Negro and Primiceri (2015).

Introduction Methodology and data Results Conclusions Beferencias	
Methodology Estimation: TVP-VAR-SV	

- The first 6 years to calibrate the priors distributions.
- Following Wang y Kwan (2021), draw 10,000 samples from the posterior distribution, discard first 2,000 samples (chain should converge).
- NRI is the conditional 5-year (long run) forecast of the observed ex ante real interest rate:

$$r_t^* = (0, 0, 1) * E_t(y_{t+20}) = (0, 0, 1) * X_t' \beta_t^{20}$$



- Benati (2020): M1 velocity is, approximately, the permanent component of the short-term rate.
- Implication: Decision of wealth allocation to non interestbearing M1, react to permanent shocks to the opportunity cost, essentially ignoring transitory shocks.
- Then, M1 velocity can be considered as a reliable estimate of the nominal NRI Benati (2023).
- Estimation of NRI based on Cochrane (1994): permanent component of GDP from consumption information.

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Introduction	
Methodology and data	
Results	
Conclusions	
Referencias	
Methodology	
Estimation: M1 velocity	

The permanent component of the nominal NRI, *R^P_t*, is determined by permanent shocks to inflation, π^P_t, and to real NRI *r^N_t*:

$$R_t^P = \pi_t^P + r_t^N$$

Under IT, permanent changes in M1 velocity reflect permanent fluctuations in the NIR, and thus:

$$V_t = \beta_1 + \beta_2 r_t^N + v_t$$



- A two-step proedure:
 - Project the monetary policy rate on M1 velocity and get estimated nominal NR.
 - Real TNI = estimated nominal TNI and the inflation target (or avergae inflation).
- Econometrically: (i) Cointegrated VAR as in Cochrane (1994),
 (ii) Projection using OLS regression.

Methodology

Assessment: SVAR with long-run restrictions

- Criterion: the NRI does not react to transitory shocks (shocks that have no long-run effect on real interest rate).
- Estimation of a two-variable VAR for the ex-ante real interest rate r_t and r_t^N .
- Identification of transitory and permanent shocks: a transitory shock has no effect on the ex ante real interest rate in the long-run.
- r_t^N is a good NRI measure if (i) the response of r_t^N to a transitory shock is close to zero, and (ii) the contribution of the transitory shock to the variance of r_t^N is very small.

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Introduction	
Methodology and data	
Results	
Conclusions	
Referencias	
Methodology	
Assessment: SVAR with long-run restrictio	ns

The VMA representation for Δr_t and Δr^N_t in terms of fundamental innovations can be written as:

$$\begin{bmatrix} \Delta r_t \\ \Delta r_t^N \end{bmatrix} = \begin{bmatrix} \bar{r} \\ \bar{r}^N \end{bmatrix} + \sum_{i=0}^{\infty} \begin{bmatrix} \phi_{11}(i) & \phi_{12}(i) \\ \phi_{21}(i) & \phi_{22}(i) \end{bmatrix} \begin{bmatrix} \varepsilon_{t-i}^P \\ \varepsilon_{t-i}^T \end{bmatrix}$$
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• Identificantion using a long-run restriction (Blanchard and Quah, 1989): an innovation to ε_t^T has no long-run effect on the ex ante real interest rate, i.e. $\sum_{i=0}^{\infty} \phi_{12}(i) = 0$.



- r_t^N is a good NRI measure if:
 - i Cumulative IRF to ε_t^T shocks is close to zero: $\sum_{i=0}^{\infty} \phi_{22}(i) \rightarrow 0$.
 - ii The contribution of ε_t^T shocks to fluctuations in r_t^N is close to zero.

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- The data obtained from the corresponding central banks.
- Peru: 1995Q4-2023Q2 for Peru, Chile: 1997Q1-2023Q2.
- Series: real GDP growth, the ex-ante real interest rate, and inflation.
- Real GDP growth: percentage changes on year-over-year basis.
- Inflation: annual growth rate of CPI excluding food and energy.

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- The ex-ante real interest rate: policy interest rate minus inflation expectations (four-quarter moving average of past inflation).
- 24 quarters used as the presample to calibrate priors and include 2 lags in the VAR, the estimated NRI starts in 2002Q2 for Peru and 2003Q3 for Chile.
- The estimation of TVP-VAR-SV was perform in R using the package "bvarsv" Krueger (2022).

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- Real interest rate as the difference between nominal interest rate and the inflation target.
- M1 velocity is the ratio between nominal GDP and M1.

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	Introduction Methodology and data	
	Results	
	Conclusions	
	Referencias	
Contents		







4 Conclusions



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Estimation of the NRI: Peru, 1995Q4-2023Q2.



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Results Estimation of the NRI: Chile, 1997Q1-2023Q2.



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Assessment: Cumulative IRF after a transitory shock.

Table. NRI estimates for Perú: Cumulative IF			
Quarter	Benati-VECM	Benati-OLS	TVP-VAR-SV
1	-0.04*	-0.03*	0.01*
2	0.00	0.00	0.01
3	0.04	0.04	0.01
4	0.09	0.07	0.01
8	-0.01	-0.01	0.00
20	0.00	0.00	0.00

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Introduction	
Methodology and data	
Results	
Conclusions	
Referencias	
Results	
Assessment: Variance decomposition	

Table. NRI estimates for Peru: Variance decomposition

Quarter	Benati-VECM	Benati-OLS	TVP-VAR-SV
1	2.98	2.98	16.99
2	4.49	4.49	10.78
3	7.37	7.37	10.10
4	9.96	9.96	9.69
8	17.43	17.43	10.38
20	17.86	17.86	10.44

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Assessment: Cumulative IRF after a transitory shock.

Table. NRI estimates for Chile: Cumulative II			umulative IRF
Quarter	Benati-VECM	Benati-OLS	TVP-VAR-SV
1	-0.02*	-0.04*	0.04*
2	-0.02*	-0.05*	0.04*
3	-0.01	-0.01	0.01
4	0.00	0.01	0.02
8	0.01	0.01	0.00
20	0.00	0.00	0.00

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Introduction	
Methodology and data	
Results	
Conclusions	
Referencias	
Results	
Assessment: Variance decomposition.	

Table. NRI estimates for Chile: Variance decomposition

Quarter	Benati-VECM	Benati-OLS	TVP-VAR-SV
1	42.66	42.66	5.74
2	36.89	36.89	5.12
3	48.59	48.59	8.38
4	49.31	49.31	8.32
8	48.68	48.68	8.67
20	49.56	49.56	8.69

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1 Introduction

2 Methodology and data

3 Results





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- We estimated and assessed two measures of NRI for Chile and Perú: (i)TVP-VAR-SV Lubik y Matthes (2015), and (ii) M1 velocity Benati (2023).
- Assessment based on identification of transitory shocks to real interest rate.
- Criterion: NRI does not react to transitory structural shocks (IRF, VD).
- Both are good measures, TVP-NRI measures are relatively superior.

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- Include Brazil, Colombia, and Mexico.
- Assess other measures, e.g. Laubach y Williams (2003) and Holston et al. (2017).

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