# XXXVI ENCUENTRO DE ECONOMISTAS DEL BANCO CENTRAL DE RESERVA DEL PERÚ 

# Capital Flows and Bank Risk-Taking 

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(1) Introduction
(2) The Competitive Equilibrium
(3) The Efficient Allocation

4 Numerical Results
(5) Conclusions

## Introduction

- 1998 Peruvian sudden stop: After 1998Q3, there is a gradual reduction of the ST NFL to GDP ratio and an almost immediate increase of the morosity ratio of the banking system. The morosity ratio jumped from 6.4 to 10.3 in three quarters.
- I provide a framework to understand the dynamics of the excessive bank risk-taking after an unanticipated sudden stop.
- I simulate the 1998 Peruvian sudden stop.

Figure 1: Morosity rate of the Peruvian banking system (\%)


Source: SBS.

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## Results

- The limited liability + deposit insurance $\Rightarrow$ Inefficiently high level of loans.
- The intertemporal effect amplifies the inefficiency.
- Sudden Stop Simulation: I assume a $87 \%$ gradual reduction of the foreign borrowing limit to account for the reduction of the ST NFL to GDP (from 7.5\% (1998Q3) to $1 \%$ in 2010).
- In the long-term:
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- This is in line with the behavior of the morosity ratio.
- When abstracting from the intertemporal effect the short-term responses are (1.1 and 1.1 respectively) and those account for the $8.5 \%$ and $6.8 \%$ of their long-term movements.


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## Model

- Infinity time period small open economy model.
- Domestic households (HHs), banks, foreign investors government. HHs own banks.
- Each period households decide how much to consume and save (only through deposits on banks).
- Banks receive deposits from HHs and foreign investors, and make risky investments.
- Assumptions:


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- Banks face limited liability.
- Domestic and foreign deposits are insured by the government.
- Banks have an exogenous binding foreign borrowing limit.
- An exogenous law of motion of the bank equity.
- Agents are risk-neutral.
- Opportunity cost of foreign investor smaller than domestic ones.


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## Domestic Households

- Utility of HHs at time $t$,

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\begin{equation*}
W_{t}=\mathbb{E}_{t}\left\{\sum_{i=0}^{\infty} \beta^{i} C_{t+i}\right\}, \tag{1}
\end{equation*}
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- $\beta$ is the HHs discount factor, $C_{t}$ is the consumption level at period $t$.
- The budget constraint at time $t$ is,

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\begin{equation*}
C_{t}+D_{t}=\omega^{H}+\bar{R}_{t-1}^{D} D_{t-1}+\Pi_{t}+T_{t} \tag{2}
\end{equation*}
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- Since I assume deposit insurance domestic depositors will also always receive the agreed gross return.
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- HHs maximize (1) subject to (2). The first order condition for $D_{t}$ requires,

$$
1=\beta \bar{R}_{t}^{D}
$$

## Banks

- The balance sheet equation,

$$
K_{t}=D_{t}+D_{t}^{F}+N_{t},
$$

- $N_{t}$ : Equity at time $t$.
- $D_{t}^{F}$ : Short-term deposits held by foreign investors (foreign deposits).
- Banks intermediate $K_{t}$ of capital in period $t$.
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- $\delta$ : capital depreciation rate.


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V_{t}=\mathbb{E}_{t}\left\{\sum_{i=0}^{\infty} \beta^{i} d_{t+i}\right\}
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- Hence, if banks default,

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- $\gamma$ : exogenous and constant across time.


## Banks

- In general,

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\begin{gathered}
d_{t+1}=\gamma\left[N_{t+1}+N_{t}\right]^{+}, \\
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- which is the law of motion of equity.
- I define $e_{t+1}^{z, *}$ :

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- If $e_{t+1}^{z}<e_{t+1}^{z, *}$, banks default. The default probability is,

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## Banks

- The Lagrangian equation is:

$$
L_{t}=\mathbb{E}_{t}\left\{\sum_{i=t}^{\infty} \beta^{i-t}\left(\gamma \frac{N_{i}}{1-\gamma}+\lambda_{i}\left[\left[(1-\delta) K_{i-1}+Z_{i} K_{i-1}^{\alpha}-\bar{R}_{i-1}^{D} D_{i-1}-\bar{R}_{i-1}^{F} \phi_{i-1}\right]^{+}(1-\gamma)-N_{i}\right]\right)\right\}
$$

- where $\lambda_{t}$ is the LM associated with the law of motion of equity
- $\lambda_{t}$ : Shadow value of bank equity. Rewriting $L_{t}$,

- The FOC for $D_{t}$ yields:


$$
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## Banks

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L_{t}=\mathbb{E}_{t}\left\{\sum_{i=t}^{\infty} \beta^{i-t}\left(\gamma \frac{N_{i}}{1-\gamma}+\lambda_{i}\left[\left[(1-\delta) K_{i-1}+Z_{i} K_{i-1}^{\alpha}-\bar{R}_{i-1}^{D} D_{i-1}-\bar{R}_{i-1}^{F} \phi_{i-1}\right]^{+}(1-\gamma)-N_{i}\right]\right)\right\}
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& \beta \int_{e_{t+1}^{z, *}}^{+\infty} \lambda_{t+1}\left[N O I_{t+1}+N_{t}\right](1-\gamma) d F\left(e_{t+1}^{z}\right)-\mathbb{E}_{t}\left\{\lambda_{t+1} N_{t+1}\right\}+\mathbb{E}_{t}\left\{L_{t+2}\right\} .
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C_{t}=\omega^{H}+(1-\delta) K_{t-1}+Z_{t} K_{t-1}^{\alpha}-K_{t}+\phi_{t}-\bar{R}_{t}^{F} \phi_{t-1}
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- The social planner aims to maximize the welfare of the domestic economy: Utility of HHs, $W_{t}$.
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K_{t}=\left(\frac{\mathbb{E}_{t}\left\{Z_{t+1}\right\} \alpha}{1 / \beta-(1-\delta)}\right)^{\frac{1}{1-\alpha}}
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Comparing the SP and CE equilibriums

- Is capital inefficiently high under limited liability (as in the two period version)?
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- In the competitive equilibrium (LL + DI ) loans are,

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Comparing the SP and CE equilibriums

- By definition $\mathbb{E}_{t}\left\{Z_{t+1} \mid e_{t+1}^{z} \geq e_{t+1}^{z, *}\right\} \geq \mathbb{E}_{t}\left\{Z_{t+1}\right\}$. From the FOCs of $D_{t}$ and $N_{t}$,

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\lambda_{t}=\int_{e_{t+1}^{z, *}}^{+\infty} \lambda_{t+1} d F\left(e_{t+1}^{z}\right)(1-\gamma)+\frac{\gamma}{1-\gamma} .
$$

- $\lambda_{t+1}$ is not independent of $e_{t+1}^{z}$. Numerical results: $\operatorname{Cov}_{t}\left\{Z_{t+1} \lambda_{t+1} \mid e_{t+1}^{z} \geq e_{t+1}^{z, *}\right\}>0$, then

$$
K_{t}^{C E}>K_{t}^{S P} .
$$

- The lower the productivity shock, $e_{t}^{z}$, the higher likelihood that banks default at $t+1$ and thus the lower the probability that an exogenous unit of bank's equity at $t$ increases bank's capacity to accumulate equity at $t+1$.
- In an infinity time period model the excess bank risk-taking is amplified:
- The excess marginal benefits of loans, $\theta_{t}$, is found in:

$$
(1-\delta)+\alpha \mathbb{T}_{t}\left\{Z_{t+1}\right\}\left(K_{t}^{C E}\right)^{\alpha-1}+\theta_{t}=R^{B} .
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$$
K_{t}^{C E}>K_{t}^{S P} .
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- The lower the productivity shock, $e_{t}^{z}$, the higher likelihood that banks default at $t+1$ and thus the lower the probability that an exogenous unit of bank's equity at $t$ increases bank's capacity to accumulate equity at $t+1$.
- In an infinity time period model the excess bank risk-taking is amplified:
- The excess marginal benefits of loans, $\theta_{t}$, is found in:



## Comparing the SP and CE equilibriums

- By definition $\mathbb{E}_{t}\left\{Z_{t+1} \mid e_{t+1}^{z} \geq e_{t+1}^{z, *}\right\} \geq \mathbb{E}_{t}\left\{Z_{t+1}\right\}$. From the FOCs of $D_{t}$ and $N_{t}$,

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$$
(1-\delta)+\alpha \mathbb{E}_{t}\left\{Z_{t+1}\right\}\left(K_{t}^{C E}\right)^{\alpha-1}+\theta_{t}=R^{B} .
$$

## Calibration

Table 1: Parameters

| Description |  | Value | Source / Target |
| :--- | :---: | :---: | :--- |
| Discount factor | $\beta$ | 0.986 | Gross domestic rate $=1.060$ (annual) |
| Gross foreign interest rate | $R^{F}$ | 1.003 | Gross foreign rate $=1.0124$ (annual) |
| Capital's shares in output | $\alpha$ | 0.330 | Standard value |
| Capital depreciation ratio | $\delta$ | 0.120 | Bank Leverage ratio |
| Dividend policy | $\gamma$ | 0.540 | Short-term dynamics of $p_{t}$ |
| Foreign borrowing limit | $\phi$ | 2.066 | NFL to GDP ratio |
| Government Expenses | $G$ | 0.975 | Bank Credit to GDP ratio |
| Households' exogenous income | $\omega^{H}$ | 3.906 | Consumption to GDP ratio |
| Mean of log Z $Z_{1}$ | $\mu_{z}$ | 0.000 | Normalized |
| Std. Dev. of the productivity shock | $\sigma_{e^{z}}$ | 0.952 | Default Probability $=3 \%$ (annual) |
| Persistence of the shock | $\rho_{z}$ | 0.850 | Standard value |

Each period represents a quarter.

## Stochastic Steady State

Table 2: Stochastic Steady State

|  |  | $(1)$ | $(2)$ | $(3)$ | $(4)$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Description | Variables | SP | CE | CE $^{\dagger}$ | CE-ULL |
| Bank leverage ratio | $K_{s s} / N_{s s}$ | - | 9.53 | 9.14 | 9.07 |
| NFL to GDP ratio (\%) | $\phi /\left(4 . G D P_{s s}\right)(\%)$ | 7.57 | 7.54 | 7.56 | 7.57 |
| Bank credit to GDP ratio (\%) | $K_{s s} /\left(4 . G D P_{s s}\right)(\%)$ | 27.49 | 28.38 | 27.63 | 27.49 |
| Consumption to GDP ratio (\%) | $C_{s s} / G D P_{s s}(\%)$ | 72.44 | 72.07 | 72.39 | 72.44 |
| NFL to credit ratio (\%) | $\phi / K_{s s}(\%)$ | 27.51 | 26.56 | 27.37 | 27.51 |
| Bank default probability (\%) | $p_{s s}(\%)$ | - | 0.74 | 0.37 | 0.32 |
| Excess marginal benefits (\%) | $\theta_{s s}(\%)$ | - | 0.31 | 0.05 | - |
|  | $K_{s s}^{C E} / K_{s s}^{S P}-1(\%)$ | - | 3.58 | 0.54 | - |

$C E^{\dagger}$ : Competitive equilibrium abstracting from the intertemporal channel, i.e. assuming $\lambda_{t}$ is independent of $e_{t}^{z}$. $C E-U L L:$ Competitive equilibrium under unlimited liability. NFL $=$ Net foreign liabilities $=\phi$. NFL to GDP ratio $=$

$$
\phi / G D P_{s s} . G P D_{s s}=G+Y_{s s} . Y_{s s}=\omega^{H}+Z_{s s} K_{s s}^{\alpha}
$$

## 1998 Sudden Stop Simulation

- The economy starts from its stochastic steady state at time $t=0$.
- The sudden stop simulation: A $87 \%$ reduction of ST NFL, $\phi$.
- This is in order to capture a reduction of the ST NFL to GDP ratio from $7.5 \%$ to $1 \%$.
- The adjustment of the borrowing limit is gradual,

$$
\log \left(\phi_{t}\right)=\rho_{\phi} \log \left(\phi_{t-1}\right)+\left(1-\rho_{\phi}\right) \log \left(\phi^{n e w}\right)
$$

- for $t \geq 1$.
- The initial fall in the foreign borrowing limit happening in $t=1$ is not anticipated by agents.
- From the period 1 on, agents correctly anticipate the path of $\phi_{t}$.
- I set $\rho_{\phi}=0.92$ in order to match the dynamics of the ST NFL to GDP ratio.


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## 1998 Sudden Stop Simulation

Figure 2: ST NFL to GDP (\%)


Data: $\mathrm{NFL}=$ short-term foreign obligations of the financial system. Model: NFL=foreign borrowing limit. Source: CRBP.

## 1998 Sudden Stop Simulation


$C E^{\dagger}$ : Competitive equilibrium when abstracting from the intertemporal channel.

## 1998 Sudden Stop Simulation

- In the long-term:
- The (quarterly) default probability moves from $0.7 \%$ to $1.8 \%$.
- The relative excess loans moves from $3.6 \%$ to $6.2 \%$.
- The excess marginal benefits increases from $0.31 \%$ to $0.52 \%$.
- In the short-term:
- This is in line with the behavior of the morosity ratio.
- When abstracting from the intertemporal effect, the short-term responses are (1.1, 1.1 and 1.1 respectively) and those account for the $8.5 \%, 6.8 \%$ and $6.5 \%$ of their long-term movements.


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## Conclusions

- The limited liability + deposit insurance $\Rightarrow$ Inefficient high level of loans.
- The intertemporal effect amplifies the inefficiency.
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- Future research: Optimal policies. Risk-averse agents.


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[^0]:    - $\gamma$ : exogenous and constant across time.

